

EXAM REVIEW 1st Semester

Unit 4: Functions

Name: _____

Hour: _____

Vocabulary:

Domain: x-values

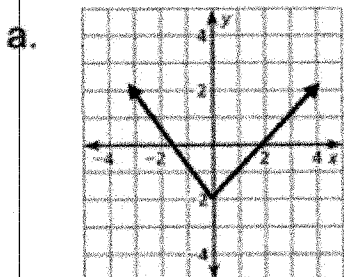
Range: y-values

Function: x cannot repeat

Function Notation: $f(a) = b$
 ↑ ↑
 x y

Practice Problems:

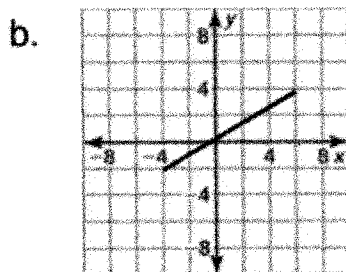
1. Find the domain and range of the function represented by the graph.



Domain: all real #'s

Range: $y \geq -2$

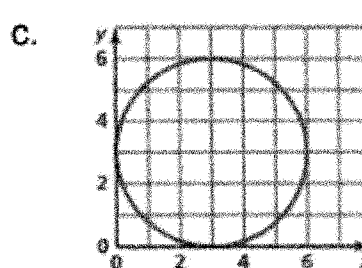
Function: yes



Domain: $-4 \leq x \leq 6$

Range: $-2 \leq y \leq 4$

Function: yes



Domain: $0 \leq x \leq 6$

Range: $0 \leq y \leq 6$

Function: NO

2. Determine if the relation is a function: If not – explain why

a.

Input, x	8	4	2	4	8
Output,	-4	-2	0	2	4

no, 4 repeats
8 repeats

b.

Input, x	0	2	4	6	8
Output,	3	7	11	15	19

yes, no x-value repeats

c. (1,2), (2,3), (2,5), (4,8)

no, 2 repeats

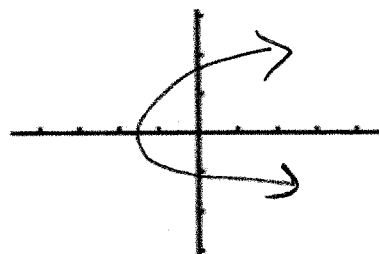
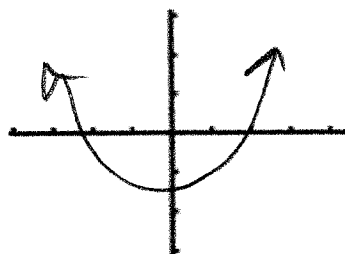
3. Write Ordered Pairs that are:

a. Function: (1,2), (2,3), (3,3)

b. Draw a Function graph:

c. Draw a NON Function graph

Non-Function: (1,2), (2,3), (2,4)



4. Solve the following:

a. $f(x) = 2x - 6$, solve for x when $f(x) = 10$

$$\begin{array}{r} 10 = 2x - 6 \\ +6 \quad +6 \\ \hline 16 = 2x \\ \frac{16}{2} = \frac{2x}{2} \end{array} \quad \boxed{x=8}$$

b. Given $h(x) = -3x - 10$, find $h(-3)$

$$\begin{array}{r} -3(-3) - 10 \\ 9 - 10 \end{array} = \boxed{-1}$$

Vocabulary:

Average Rate of Change: $\frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x}$

Practice Problems:

5. Given the following data, find the average rate of change between:

a. $x = -1$ and $x = 1$

x	-1	0	1
s(x)	0	3	6

$$\frac{6 - 0}{1 - (-1)} = \frac{6}{2} = \boxed{3}$$

b. $x = 2$ and $x = 4$

x	0	2	4
t(x)	8	4	0

$$\frac{0 - 4}{4 - 2} = \frac{-4}{2} = \boxed{-2}$$

Vocabulary:

Piecewise Functions: a function in several pieces

Practice Problems:

6. Graph the following function and answer the questions below:

$$f(x) = \begin{cases} 0, & 0 < x < 5 \\ 5, & 5 \leq x < 11 \\ 7, & 11 \leq x < 16 \end{cases}$$

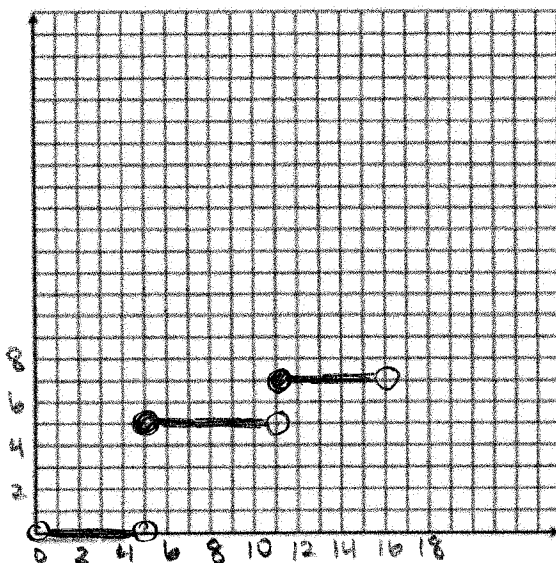
\uparrow \uparrow
 value value

Evaluate:

b. $f(5) = 5$

c. $f(12) = 7$

d. $f(0) = \text{undefined}$



Vocabulary:

Absolute Value function: $f(x) = |x|$



Patterns of shifting the graph:

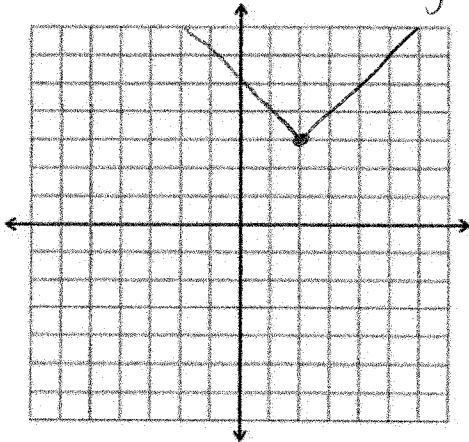
x

y

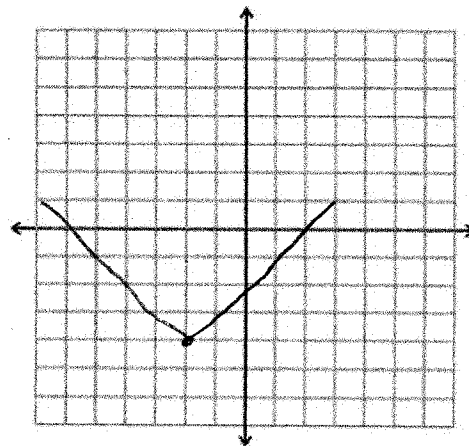
Practice Problems:

7. Graph the following equations

a. $g(x) = |x - 2| + 3$
 $\xrightarrow{\text{up } 3}$
 $\xrightarrow{\text{right } 2}$

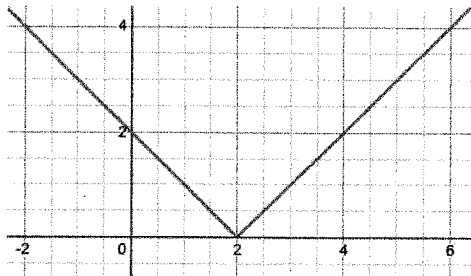


b. $f(x) = |x + 2| - 4$
 $\xrightarrow{\text{left } 2}$
 $\xrightarrow{\text{down } 4}$



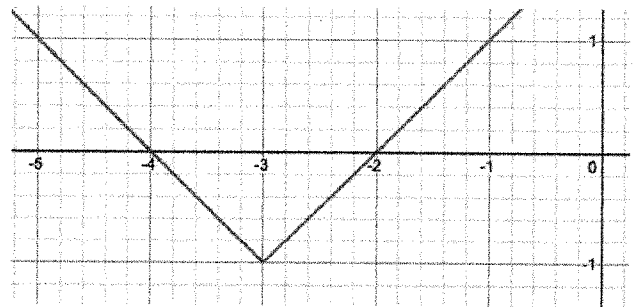
8. Write the equations for the following graphs:

a.



$f(x) = |x - 2|$

b.



$f(x) = |x + 3| - 1$

Vocabulary

Inverse Function

Solve for the other variable

Practice Problems:

9. Find the inverse function

a. $m = 3g + 10$

$\frac{m-10}{3} = \frac{3g}{3}$

$g = \frac{m-10}{3}$

b. $g = \frac{3w}{10} + 10$

$\frac{10g}{3} = \frac{3w}{3} + 30$

$w = \frac{10g}{3} - 30$

c. $f = 2(3x - 2)$

$f = 6x - 4$

$\frac{f+4}{6} = \frac{6x}{6}$

$x = \frac{f+4}{6}$